
Design of Experiments in Ecological and Environmental Problems: methods and issues

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Outline

- Problem statement
 - Implementation problems
 - Simulation Example
 - Some applicable DOEs
 - Other modeling alternatives
 - Applications/extensions
 - PASI in Latin America
 - Conclusions
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Problem statement

- Complexity of Environmental Problems
 - Too many variables in the system
 - Interactive/non linear structure
 - Difficulty in conducting experimentation
- Proposed solutions
 - Implement Design of Experiments (DOE)
 - In the Laboratory or with simulation models
 - EVOP approaches to experimentation

Examples of Environmental Projects

- Salinity, Ph., temperature, invasive species
 - In the survival of indigenous species
- Best mining and agricultural practices
 - In the life (length, quality) of specific species
- Contaminants, light, water velocity, flora
 - On indigenous species of the ecosystem
- Dam building and ecosystem destruction
- Difficulty to experiment in real environment
 - Or to re-create the complete environment in lab

An Industrial Experiment Example

- Duress of bathroom tiles
 - Factors: time, temperature and concentration
 - Responses: average duress, variation
- Methods of experimentation
 - Lab: bake tiles in furnace at factor levels
 - Use actual tile manufacturers
 - In different places, that use different factors
- Problems associated with both approaches
 - Reproducing original conditions and inclusion

DOE Definition

- DoE consists in the planning activities for organizing and carrying out the “best” strategy for testing a statistical hypothesis
 - Definition Keywords:
 - planning activities (before the event)
 - best strategy (seeks optimization)
 - hypothesis testing (statistical analysis)
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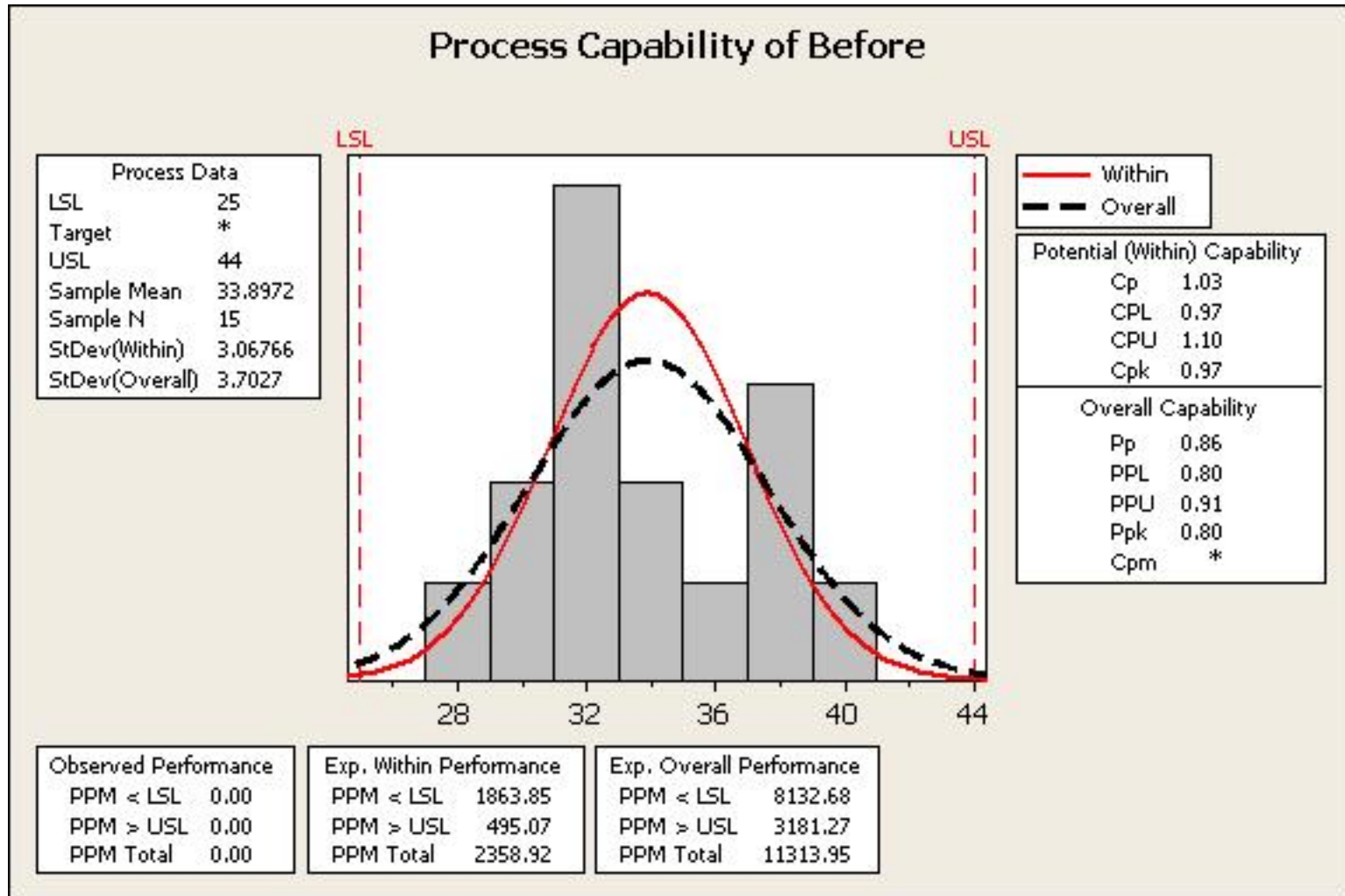
Steps to Perform DOE

- Set experimental objectives
 - Select process variables
 - Select an experimental design
 - Execute the experimental design
 - Check that data are consistent with experimental design assumptions
 - Analyze and interpret results
 - Conclude/Restart the loop
-

DOE Responses can be:

- Location parameter: average life length, number of individuals per unit, etc.
- Dispersion parameter: variance or standard deviation of life length, of individuals per unit.
- Certain factors impact variation, not location
- Variation has many useful applications
 - Comparison with upper/lower specification limits
- Variation is often slighted or ignored

Analyzing Variation as a Key Factor



Process Capability Indices:

$$C_p = \frac{U - L}{6\sigma}$$

$$C_{pk} = \frac{\text{Min}[U - \mu; \mu - L]}{3\sigma}$$

$$C_{pm} = \frac{U - L}{6\sqrt{\sigma^2 + (\mu - T)^2}}$$

$$C_{pmk} = \frac{\text{Min}[U - \mu; \mu - L]}{3\sqrt{\sigma^2 + (\mu - T)^2}}$$

Design of Experiments

- DoE considers several important issues:
 - desired precision of the results
 - significance level we can absorb
 - sample size required by problem
 - sampling schemes and estimators
 - This requires the manipulation of the Factors
 - Before Experimentation Begins
 - Not always possible in environmental work
-

Planning a DoE Involves

- Determination of the response(s) Y
 - Determination of the factors ($X_1, X_2, X_3, X_4, \dots$)
 - Determination of the model functional form
 - Determination of the interaction forms ($X_1 * X_2$)
 - Determination of the sample size (runs)
 - Determination of the experimental precision
 - Determination of the error we can absorb
 - Determination of the randomization plan
-

Model Hypotheses are:

- Educated guesses
 - The result of experience or observation
 - They are obtained by:
 - Restating the problem in statistical terms
 - They are either true or false
 - The Null and Alternative hypotheses
 - Null (H_0): always the status quo
 - Alternative (H_1): negation of the Null!
-

Some Modeling Problems

- What if variances are different?
 - Power of the test in experimental design
 - Errors (α, β) provide the sample size
 - Blocking when there are too many factors
 - Assessing model assumptions (validation)
 - What happens with model violations?
 - How can we resolve such problems?
 - Not always done, or done incompletely
-

Choice of Sample Size

- Important Experimental Design Problem!
 - Can be obtained by pre-specifying:
 - The precision of the experiment δ
 - Probabilities of types I and II errors (α, β)
 - Knowing the population variances σ^2
 - Obtain the required percentiles (z_α, z_β)
 - corresponding to the respective table values
 - for the respective probabilities $(1-\alpha)$ and $(1-\beta)$
-

Assessing Model Assumptions

- Data Independence
 - Normality of the data
 - Homogeneity of variances
 - DOE Results are only valid
 - when all assumptions hold true
 - Check graphically, at the very minimum
 - Robustness: degree of test validity under model assumption departures
-

Assumption Violations

- Lack of independence
 - Heterogeneous variances
 - Non-Normality of data
 - transformation of the data (Log, square root)
 - alternative non parametric procedures
 - Always check model assumptions
 - At least graphically
 - to insure validity of your results!
-

Three types of DOE experiments

■ Laboratory Experiments

- ❑ Not always possible to reproduce the situation
- ❑ Certain elements may not be included
- ❑ Missing factors and their interaction
- ❑ That can also affect the response

■ Simulation Experiments

- ❑ Not always possible to model complete situation

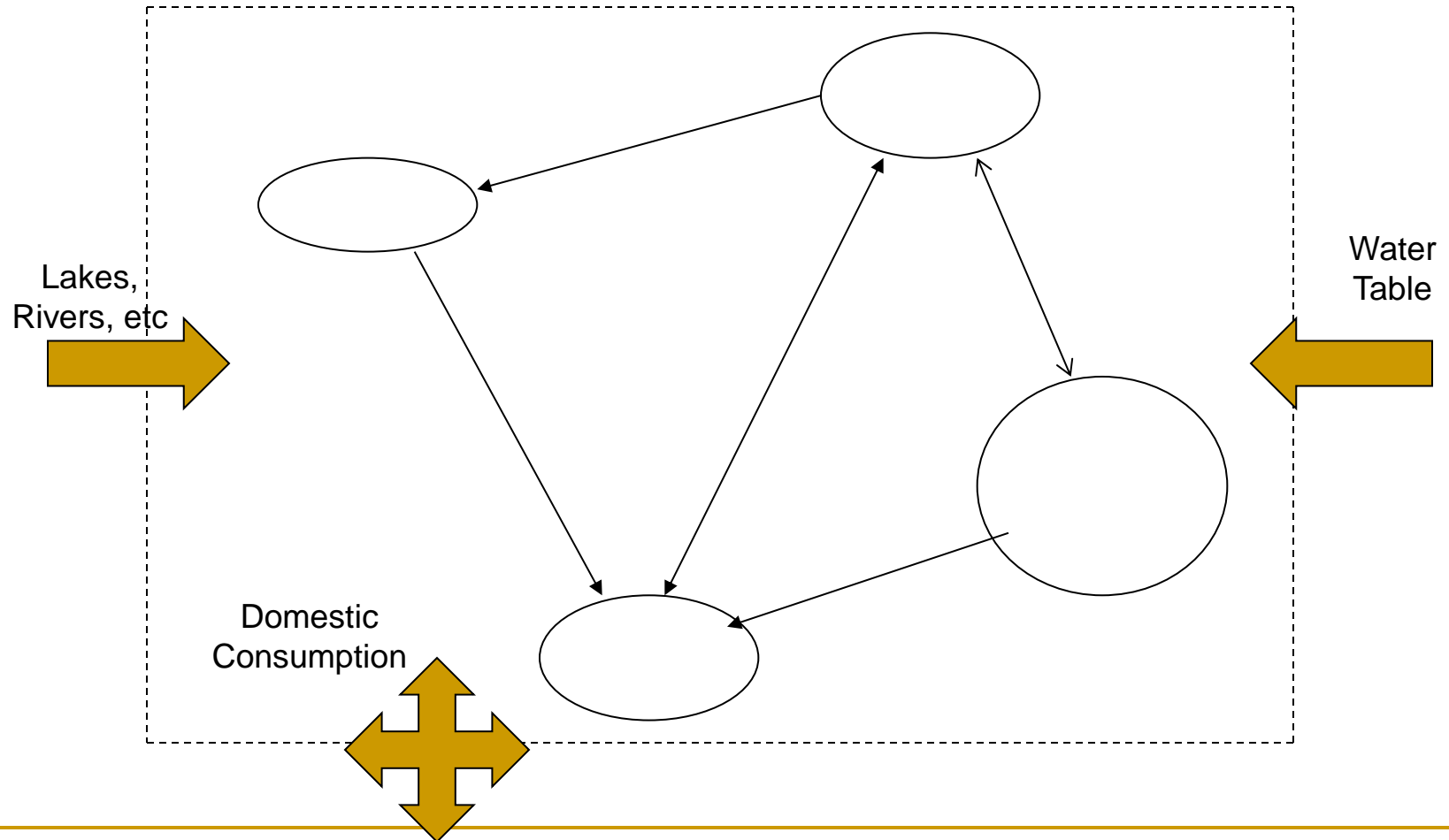
■ EVOP (Evolutionary operations)

- ❑ Not entirely under experimenter's control

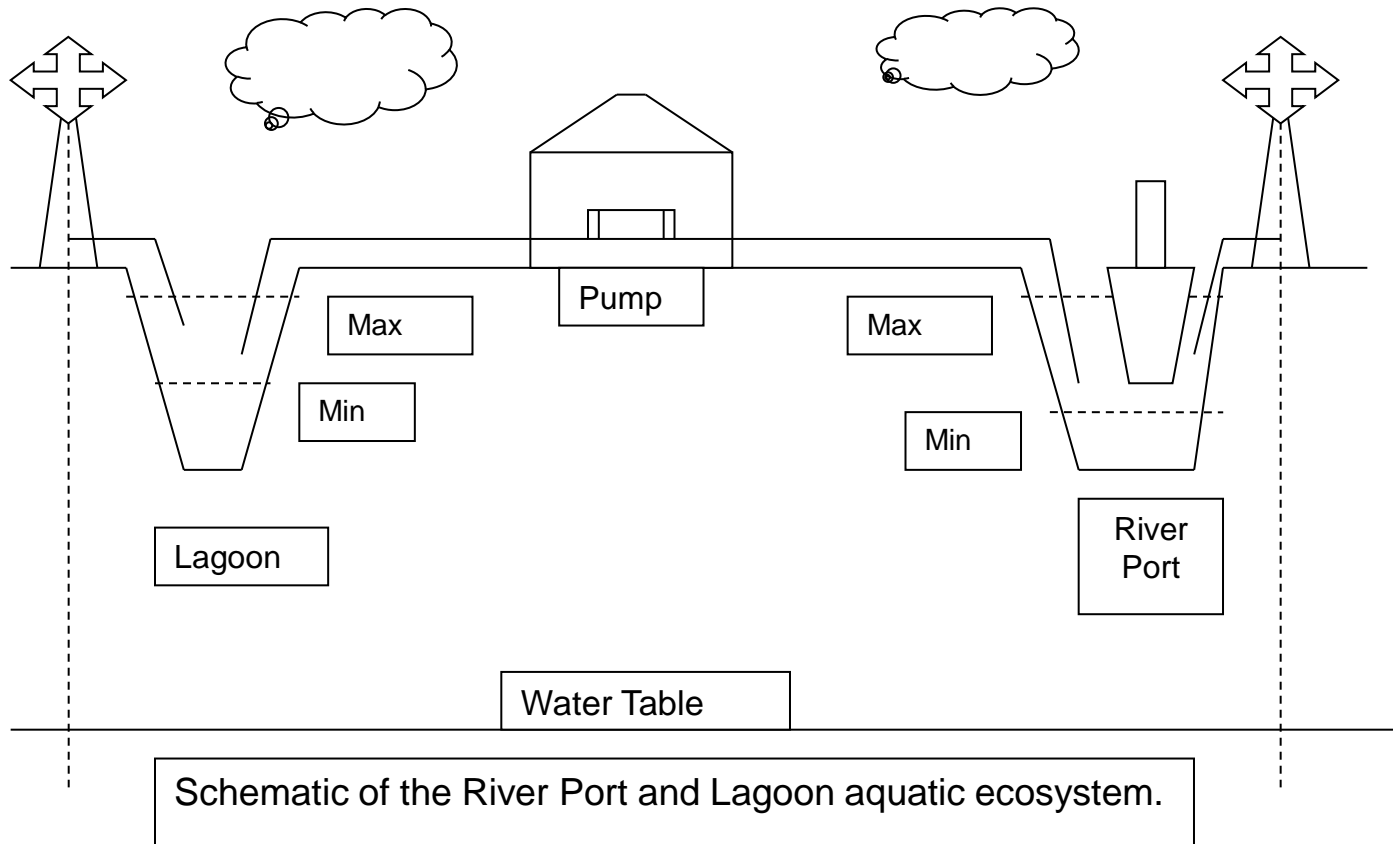
A Simulation Experiment Example

- Given a network of water masses
 - For both, civilian and industrial use
 - Optimize some performance measures
 - e.g. operational, social, political, ecological
 - Subject to a set of (conflicting) political, labor, socio-economic, etc. constraints
 - Maintaining levels of production, employment
 - Tax revenues, social services, economic, etc.
-

A Network of Interconnected Water Masses



Example: River Port w/Lagoon



Controlled Variables: Economic

- Replenishing Levels (MIN)
 - Reservoir Capacity (MAX)
 - Ordering Schedule
 - Transfer Policy
 - Usage Policy
 - Shortage Policy
 - Profitability
 - System's Initial Conditions
-

Controlled Variables: Social

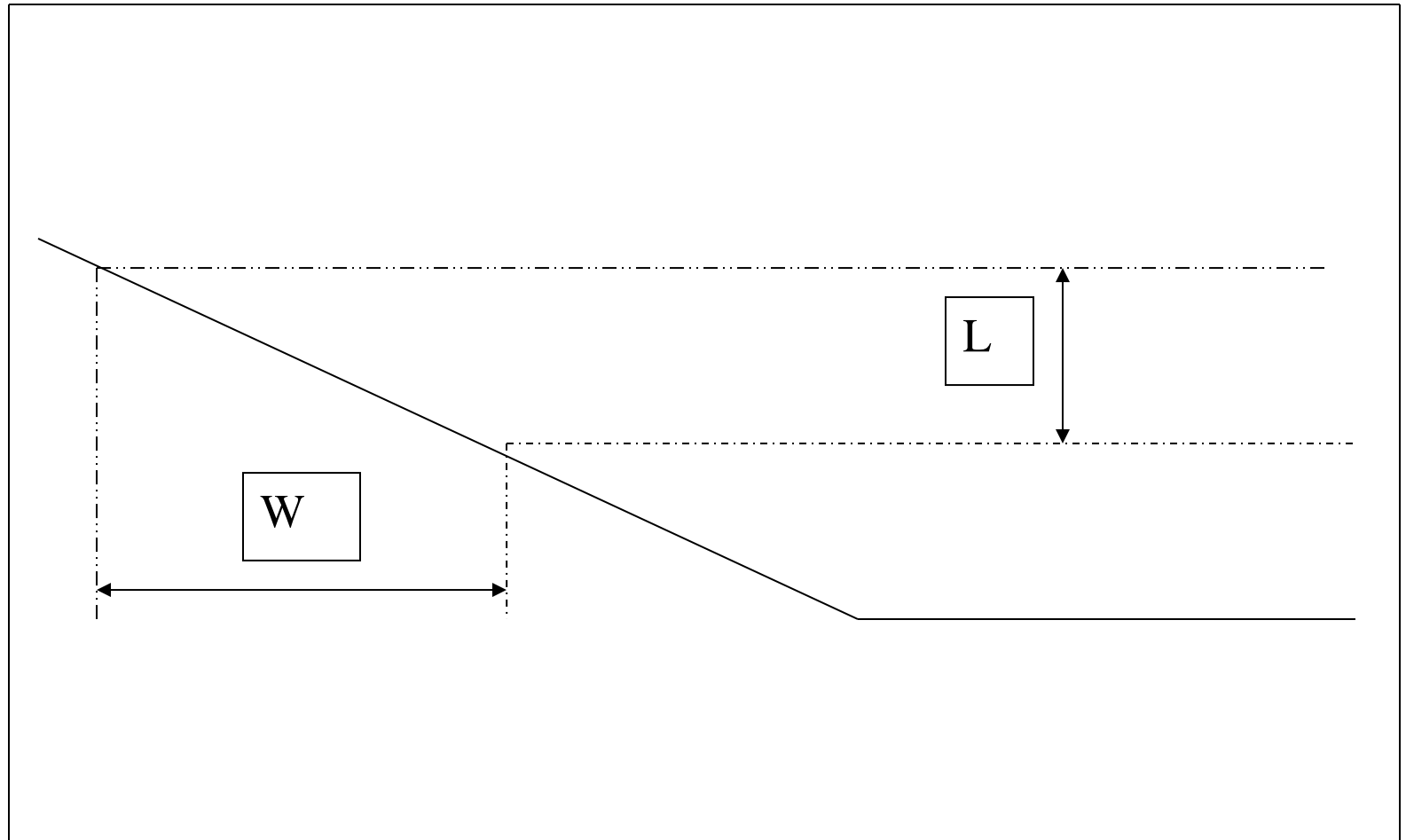
- Allocation to each sector
 - Size of the Reservoirs
 - Transfer Policy
- Generation of electricity
 - Hospitals and schools
 - Transportation uses
 - Recreation uses



Controlled Variables: Ecologic

- Wetland Area
 - Wetland Depth
 - Transfer Speed
 - Water Table Use
 - Pollution Level
 - Fish/Foul Population
-

WetLand v. Level



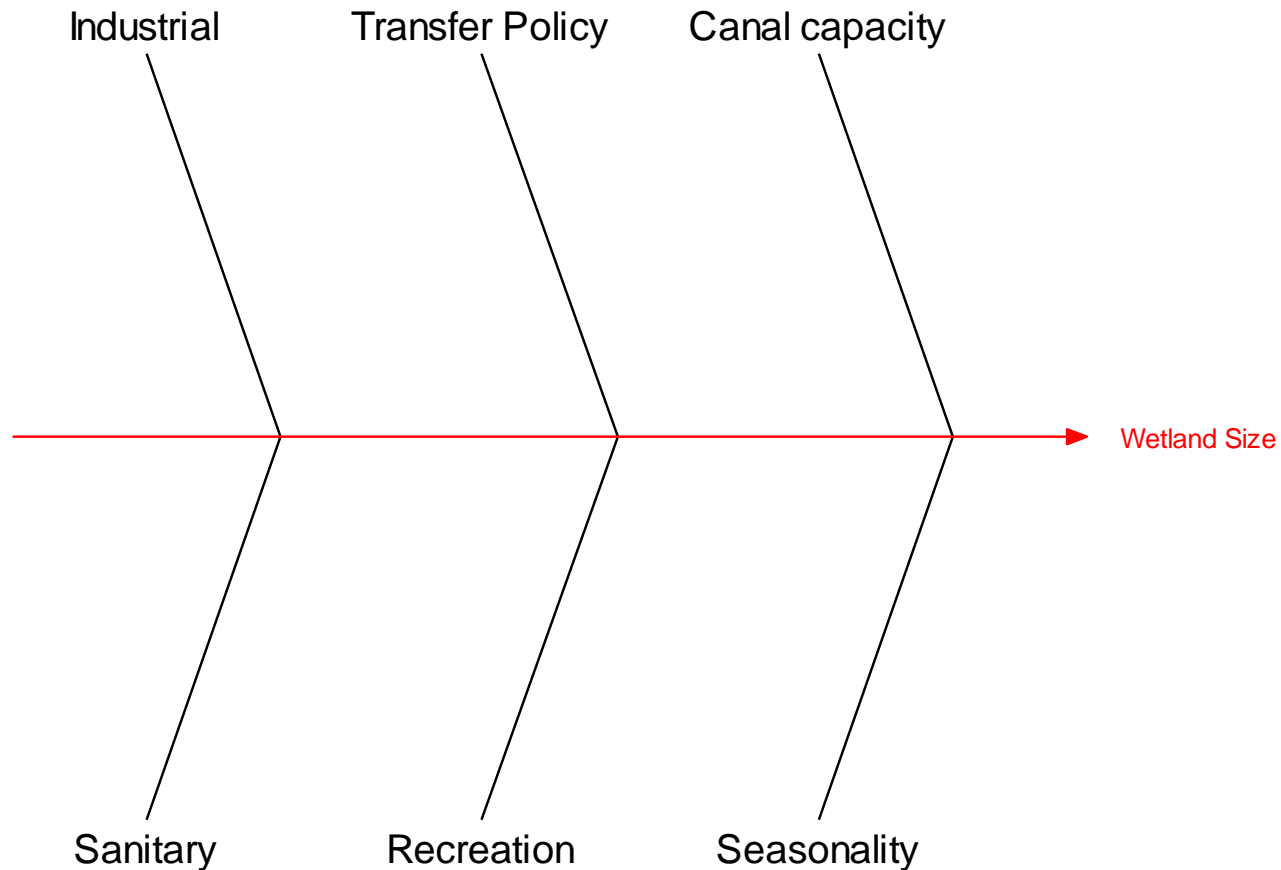
Uncontrolled Variables

- ECONOMIC
 - Political issues
 - Labor issues
 - Water Theft
 - Water Leaks
 - Markets
 - Financial
 - ECOLOGIC
 - Evaporation
 - Temperature
 - Salinity
 - Reproduction
 - Weather
 - Water Table
-

And Associated Costs

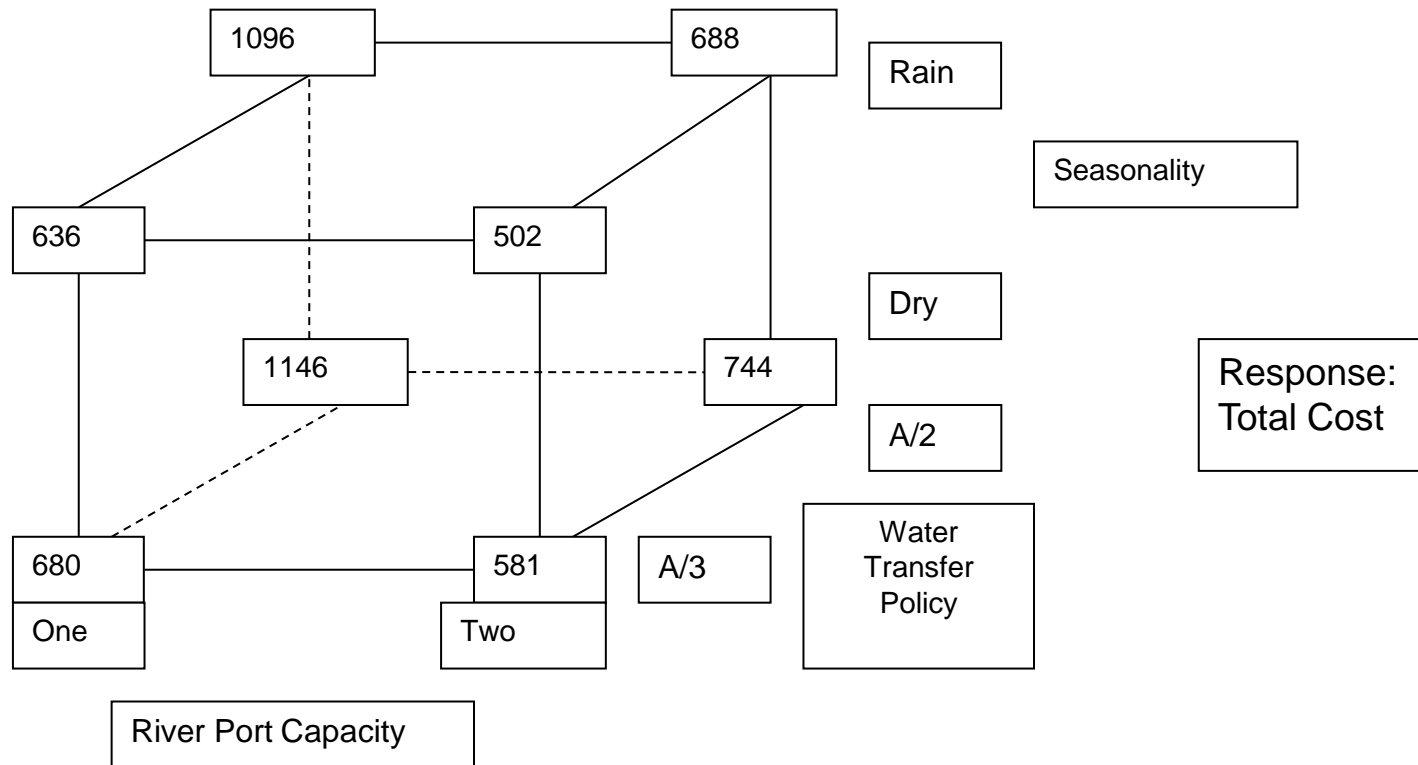
- Of Importing Water from other places
 - Transferring from Social to Economic
 - Allocation to various constituencies
 - Of Water shortages and rationing
 - Indirect costs (labor, political, social)
 - Ecological costs (degradation, loss)
 - Total costs (compound response)
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Simulation of Finger Lakes Ecosystem



Example of a Simple DOE

Complete Factorial Experiment for the Simulation

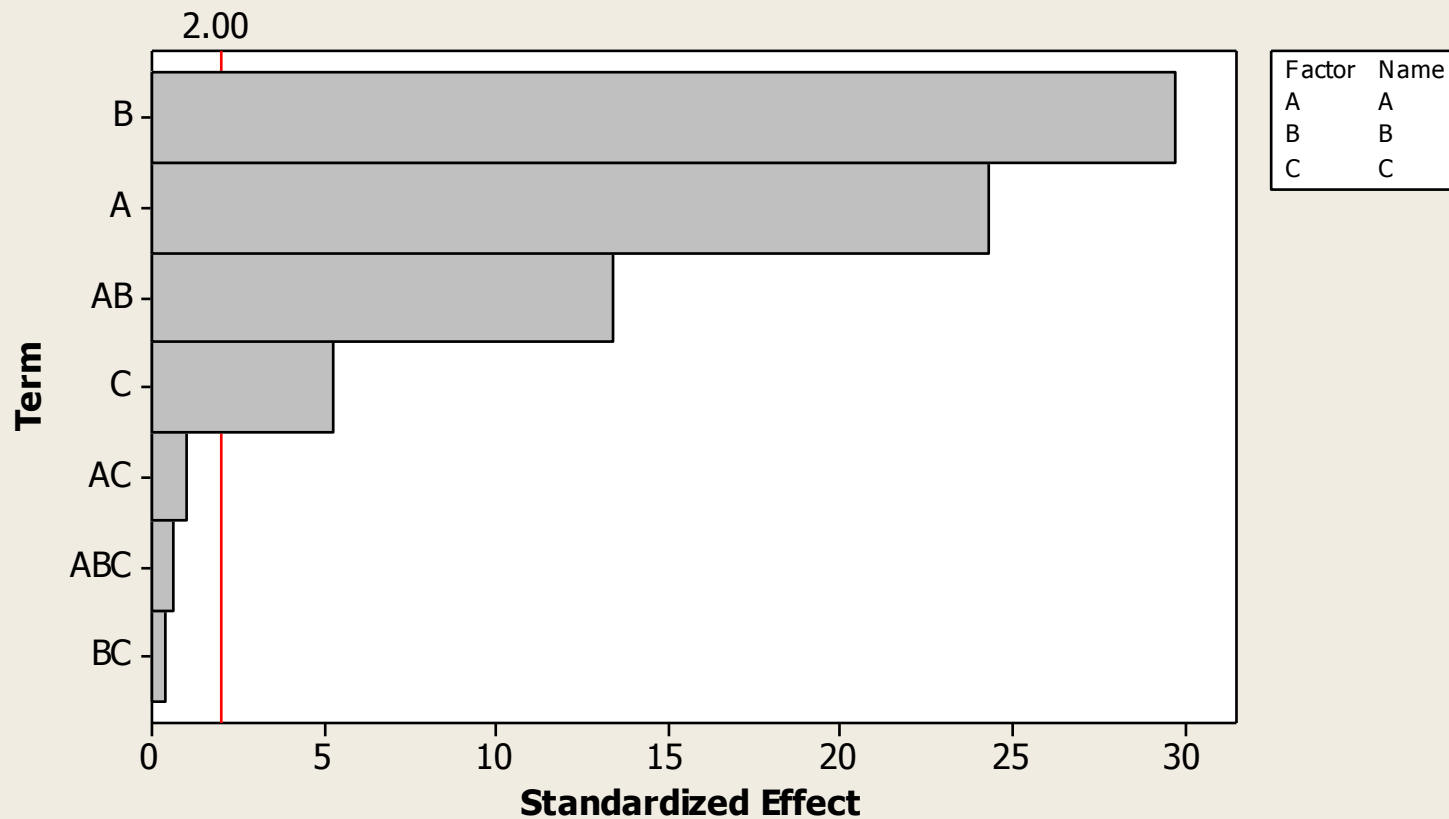


Experimental Results

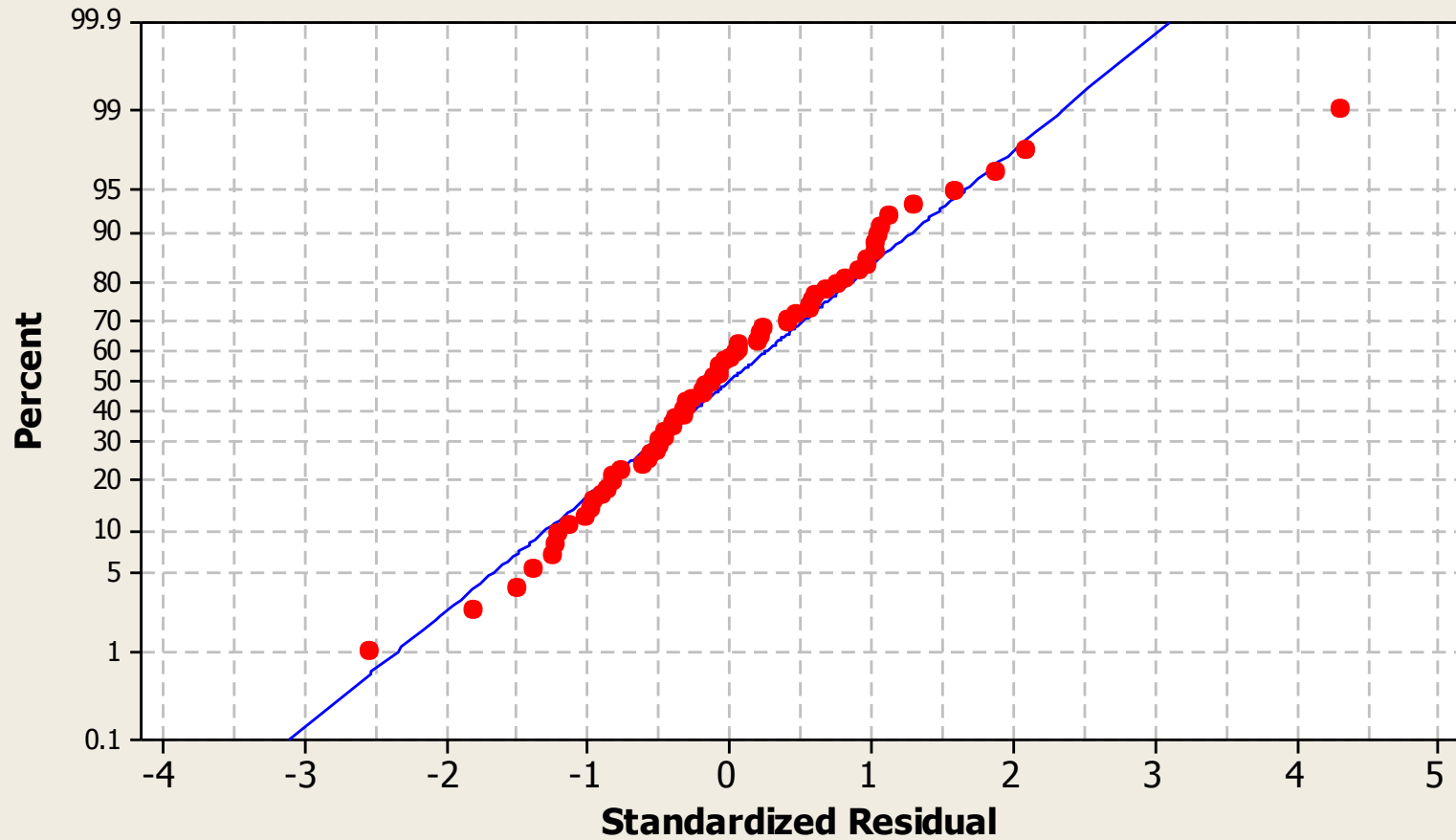
- Factor 1: Ecosystem capacity
 - of the Lake
 - of the River Canal
- Factor 2: Water Transfer Policy
 - between water masses and Water Table
- Factor 3: Seasonality (Spring/Fall)
- Interaction: $F1 * F3$
- All other variables were non-significant

Pareto Chart of the Standardized Effects

(response is Stack, Alpha = .05)



Normal Probability Plot of the Residuals (response is Stack)



Statistical Results

Table 2: Analysis of Variance Table for the Simulation Experiment

Source	D. F.	Mean Square	F Value	P-Value
River Canal Capacity	1	1219401	588.71	0.000
Water Transfer Policy	1	1828892	882.96	0.000
Seasonality (Spring/Fall)	1	58186	28.09	0.000
Enviro-Site x Policy	1	373104	180.33	0.000

Table 3: Examples of model-derived quantitative information

Factor	Change Effected	Effect on Response
River Canal Capacity	One to two ships capacity	Size decreases
Water Transfer Policy	Transfer: 1/3 to 1/2 of water mass availability	Size increase:
Seasonality	Spring into Fall Season	Size decreases
Capacity x Seasonality	Spring/one ship; Fall/Two	Size decreases:

Some Modeling Applications

- Design and Optimization of Systems
 - Identification of System Key Factors
 - Analysis of System Key Factors
 - Arbitration and Conflict Resolution
 - Evaluation of Decisions/Strategies
 - Evaluation of Robust Strategies
 - Trade-offs and Sensitivity Analyses
 - What-if, Time to catastrophic fails, etc.
-

Composite Objective Functions

Ecologic: X_i is number of occurrences of i th item:

$$f(x_1, \dots, x_p) = \sum_i v_i x_i; .with : \sum v_i = 1$$

Economic: $Y_i = a_i X_i$ is cost of No. i th item occurrences:

$$g(x_1, \dots, x_p) = \sum_i \lambda_i y_i; .with : \sum \lambda_i = 1$$

$$l(w_1, \dots, w_n) = \sum_i \delta_i w_i; .with : \sum w_i = 1$$

Arbitration and Trade-Off: α is the preference or weight:

$$H(g, l) = \alpha g + (1 - \alpha)l; .with : 0 < \alpha < 1$$

Example of modeling approach:

- Minimize Total Water Operations Cost
 - Subject to:
 - Maintaining specified labor levels
 - Reducing pollution to specified levels
 - Maintaining specified social levels
 - Maintaining specified consumption levels
 - Increasing overall health indices
-

Trade-Off Examples

Scenario	Ecologic	Health	Industry	Education	Recreation	Other
Best Ecologic	X1	Y1	Z1	W1	L1	M1
Best Health	X2	Y2	Z2	W2	L2	M2
Best Industry	X3					
Best Education	X4					
Best Recreation	X5					
Best Other	X6					

Analyze Maxi-min and
Mini-max results

Some DOE Model Limitations:

- Analyzes limited variables (here, $k=3$)
 - For, 2^K Factors/Interacts are generated
 - The Effect of Interaction, when $k > 2$
 - Can affect results, if present and strong
 - Need to find Robust Responses
 - Handling specific “noise variables”
 - Need to Identify “significant few” variables
 - To reduce model Size, maintaining Info level.
-

Consequences ... and Solutions

- Large number of factors to analyze
 - Strong factor interaction may exist
 - Dependent on the model structure
 - Requires special methods for analysis
 - Different objective of models derived:
 - To describe/study, forecast or control
 - Robust Parameter analysis capability
 - To derive a response equation that is
 - Resilient to “noise” or uncontrolled factors
-

Some Variable Id Methods

- Full Factorial Designs
 - Fractional Factorial Designs
 - Plackett-Burnam Designs
 - Latin Hypercube Sampling
 - Regression Selection methods
 - Principal Components/PCA
 - Other modeling approaches:
 - Taguchi Methodology
-

Full Factorials

- Most expensive (in time and effort)
 - Prohibitive with current number of factors
 - Most comprehensive information
 - Provides info on all factor interactions
 - Two Examples with a 2^3 Full Factorial
 - First case: mild interaction (AB only)
 - Second: strong and complex interaction
 - Notice how the Model-Estimations vary
-

Example 2^3 Full Factorial Design:

- **Variables Used**

- A = Replenishing Levels (MIN)
 - B = Reservoir Capacity (MAX)
 - C = Transfer Policy
 - Mild interaction assumed
 - A* B only
-

Full Factorial Experiment 2³

Run	A	B	C	AB	AC	BC	ABC		Avg.
1	-1	-1	-1	-1	1	1	1	-1	-1.07
2	1	-1	-1	-1	-1	-1	1	1	3.72
3	-1	1	-1	-1	-1	1	-1	1	-0.58
4	1	1	-1	-1	1	-1	-1	-1	12.04
5	-1	-1	1	1	1	-1	-1	1	7.75
6	1	-1	1	1	-1	1	-1	-1	15.45
7	-1	1	1	1	-1	-1	1	-1	11.09
8	1	1	1	1	1	1	1	1	18.31
TotSum									66.71
Effect	8.08	3.75	9.62	1.84	-0.62	-0.65	-2.08		

Regression Estimations

RegCoef	A	B	C	AB	b0
Estimat.	4.04	1.88	4.81	0.92	8.34
TRUE	4	2	5	1	10

Meta Model: $Y_{ijkl} = 8.33 + 4.04A + 1.88B + 4.81C + 0.92AB$

True Model: $Y = 10 + 4*A + 2*B + 5*C + AB + \varepsilon$

Mild Interaction (AB only)

Fractional Factorial Designs

- Analyzes only a Fraction of Full Factorial
 - Reduces substantially time/effort
 - Confounding of Main Effects/Interactions
 - If Interactions present, this is a problem
 - Only for Powers of Two (no. of runs)
 - Numerical Example: Half Fractions
 - Of the previous Full Factorial –and others
 - Assess Model-Estimation agreement
-

Fractional Factorials

First Fraction: L1

Run	A	B	C=AB	Avg.
1	1	-1	-1	-0.33
2	-1	1	-1	-0.33
3	-1	-1	1	-0.33
4	1	1	1	1.00
TotSum				0.00
Effect	7.429	3.130	11.460	
Signif.	No	No	Yes	

$$Y_1 = 7.3 + 3.71A + 1.57B + 5.73C^*$$

C *: Factor C is confounded with AB

Second Fraction: L2

Run	A	B	C=AB	Avg.
1	-1	-1	-1	-1.00
2	1	1	-1	0.33
3	1	-1	1	0.33
4	-1	1	1	0.33
TotSum				0.00
Effect	8.728	4.375	7.784	
Signif.	Yes	No	Yes	

$$Y_2 = 8.33 + 4.36A + 2.18B + 3.89C^*$$

Untangling Confounded Structure

(L1+L2)/2	8.079	3.753	9.622
(L1-L2)/2	-0.649	-0.623	1.838
Effects	8	4	10

Notice how, by averaging both Half Fraction results, we obtain the Full Factorial results again.

$$\text{True Model: } Y = 10 + 4^*A + 2^*B + 5^*C + AB + \varepsilon$$

Re-analyzing the 2^3 Full Factorial: The same Variables are used, but With Stronger Interaction

- A = Replenishing Levels (MIN)
 - B = Reservoir Capacity (MAX)
 - C = Transfer Policy
 - Stronger interaction assumed
 - $A*B$, $A*C$, $B*C$
 - Overall: $A*B*C$
-

Full Factorial: Complex, Stronger Interaction

Variables	Model Parameters						
	A	B	C	AB	AC	BC	ABC
RegCoef	3	-5	1	-12	8	-10	-15
RegEstim	1.94	-4.38	1.73	-12.14	7.34	-10.52	-15.26
MainEffEst	3.88	-8.76	3.47	-24.28	14.68	-21.05	-30.51
MainEffects	6	-10	2	-24	16	-20	-30

Var. of Model	12.5173	StdDv	3.53799
Var. of Effect	2.0862	StdDv	1.44437
Student T (0.025DF)	2.47287		
C.I. Half Width	3.57177		

Factor	A	B	C	AB	AC	BC	ABC
Signific.	Yes	Yes	No	Yes	Yes	Yes	Yes

True Model and Estimated Meta Model:

$$Y = 3A - 5B + C - 12AB + 8AC - 10BC - 15ABC$$

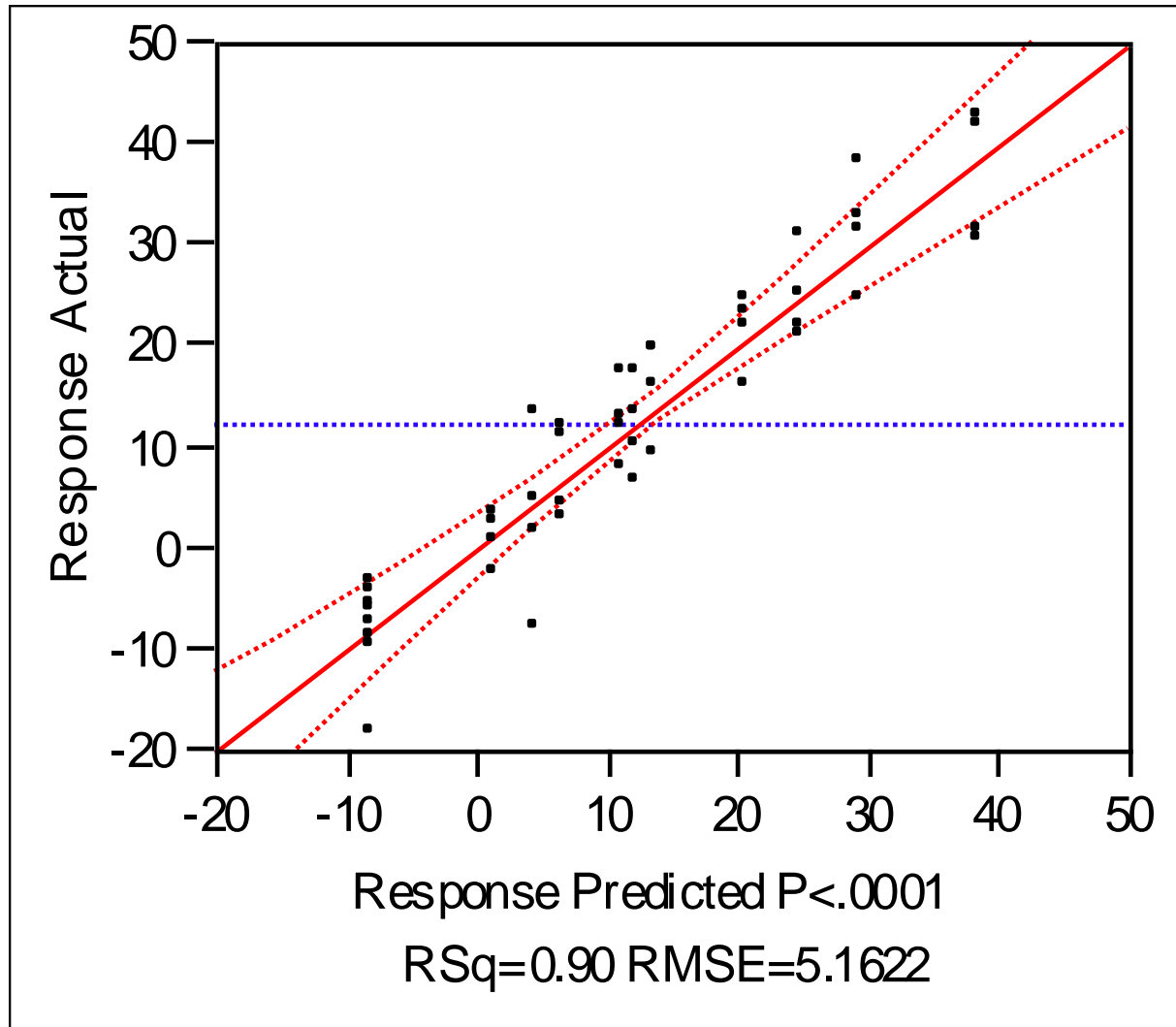
RegEstim	1.94A	-4.38B	1.73C	-12.14AB	+7.34AC	-10.52BC	-15.26ABC
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Corresponding Half Fractions

Run	Half			Analysis:						
	A	B	Fraction First C=AB	Half(a)						
				Y1	Y2	Y3	Avg.	Var	Model	
2	1	-1	-1	-15.03	-16.54	-16.04	-15.87	0.59	-14	
3	-1	1	-1	7.18	9.21	5.28	7.22	3.87	6	
5	-1	-1	1	-16.75	-19.75	-22.02	-19.51	6.97	-22	
8	1	1	1	-31.61	-27.62	-33.04	-30.76	7.89	-30	
TotSum				-56.21	-54.7	-65.82	-58.91	19.32		
Effect	-17.17	5.92	-20.81		ModlVar.	4.83	StdDev=	2.2	EffVar	
Signif.	Yes	Yes	Yes		T(.975,df)	2.75	CI-HW=	3.49	StdDev	
Run	Second			Half(b)						
	A	B	Fraction C=-AB	Y1	Y2	Y3	Avg.	Var	Model	
1	-1	-1	-1	-5.64	-0.28	9.43	1.17	58.32	2	
4	1	1	-1	4	1.47	2.49	2.65	1.62	2	
6	1	-1	1	49.73	54.94	56.86	53.84	13.62	54	
7	-1	1	1	5.99	7.88	2.56	5.48	7.26	2	
TotSum				54.08	64.01	71.34	63.14	80.82		
Effect	24.92	-23.44	27.75		ModlVar.	20.2	StdDev=	4.49	EffVar	
Signif.	Yes	Yes	Yes		T(.975,df)	2.75	CI-HW=	7.14	StdDev	
(a+b)/2	3.88	-8.76	3.47	MainEff	"C"					
(a-b)/2	-21.05	14.68	-24.28	Interact	C=AB					
Coefs	6	-10	2							

NOTE: FRACTIONAL FACTORIAL RESULTS, GIVEN THE STRONG INTERACTIONS, ARE POOR.

Plot Real vs. Prediccion



Plackett-Burnam (PB) Designs

- Are Fractional Factorial (FF) DOEs
 - Analyses “holes” between adjacent FFs
 - Reduces time/effort, considerably
 - Confounding of Main Effects/Interactions
 - Numerical Example: 11 main effects
 - Compare PB to a 2^{11} Full Factorial
 - Not all Interactions are strong/significant
 - Counter Example: strong interactions
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Plackett-Burnam w/o Interaction

- A=Replenishing Levels (MIN)
 - B=Reservoir Capacity (MAX)
 - C=Ordering Schedule
 - D=Transfer Policy
 - E=Allocation to each sector
 - F=Size of the Reservoirs
 - G=Generation of electricity
 - H=Hospitals and schools
 - I=Wetland size
 - J=Water Table
 - K=Fish/Foul Population
-

Plackett-Burnham Design (no interaction)

Run	A	B	C	D	E	F	G	H	I	J	K	Avg	
1	1	-1	1	-1	-1	-1	-1	1	1	1	-1	1	36.14
2	1	1	-1	1	-1	-1	-1	-1	1	1	1	-1	24.39
3	-1	1	1	-1	1	-1	-1	-1	-1	1	1	1	0.5
4	1	-1	1	1	-1	1	-1	-1	-1	-1	1	1	-5.96
5	1	1	-1	1	1	1	-1	1	-1	-1	-1	1	2.62
6	1	1	1	-1	1	1	1	-1	1	-1	-1	-1	31.26
7	-1	1	1	1	-1	1	1	1	-1	1	-1	-1	21.12
8	-1	-1	1	1	1	1	-1	1	1	-1	1	-1	-10.54
9	-1	-1	-1	1	1	1	1	-1	1	1	-1	1	15.92
10	1	-1	-1	-1	-1	1	1	1	-1	1	1	-1	12.02
11	-1	1	-1	-1	-1	-1	1	1	1	-1	1	1	7.33
12	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	11.66
Factors	A	B	C	D	E	F	G	H	I	J	K	Bo	
RegCoef	6	2	0	-4	-6	0	-2	4	8	-8	0	12	
RegEst.	4.5	2.3	-0.1	-4.3	-3.6	1.4	-0.8	5.2	6.1	-7.6	-2.8	12.2	
MainEff	12	4	0	-8	-12	0	-4	8	16	-16	0	n/a	
EstimEff	9.1	4.7	-0.2	-8.6	-7.2	2.8	-1.5	10.4	12.3	-15.2	-5.6	12.2	
Signific.	Yes	Yes	No	Yes	Yes	No	No	Yes	Yes	Yes	Yes	Yes	

Plackett-Burnam with Strong Interaction

- A=Replenishing Levels (MIN)
 - B=Reservoir Capacity (MAX)
 - C=Ordering Schedule
 - D=Transfer Policy
 - E=Allocation to each sector
 - F=Size of the Reservoirs
 - G=Generation of electricity
 - H=Hospitals and schools
 - I=Wetland size
 - J=Water Table
 - K=Fish/Foul Population
-

Model with Strong Interaction Structure

Factors	A	B	C	D	E	F	G	H	I	J	K	Bo
RegCoef	6	2	0	-4	-6	0	-2	4	8	-8	0	12

$$\text{Interaction: } 2*A*B - 4*H*I + G*J + D*E$$

Plackett-Burnam (n=12 rows) Analysis Results:

Factors	A	B	C	D	E	F	G	H	I	J	K	
MainEff	12	4	0	-8	-12	0	-4	8	16	-16	0	
FacEstim	-98.6	61.1	41.3	-86.5	98.4	66.4	79.7	51.8	-26.6	37.6	-96.0	
RegPar.		6	2	0	-4	-6	0	-2	4	8	-8	0
RegEstim	-49.3	30.5	20.6	-43.2	49.2	33.2	39.8	25.9	-13.3	18.8	-48.0	
Signific.	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	

Results are seriously confounded and numerically erroneous.

There are two groups of significant variables after Plackett-Burnham:

Positive: B, C, E, F, G, H, J;

and

Negative: A, D, I, K.

We Perform a Resolution IV FF
To one of the two groups

Re-Analyzing the Group of Positive Variables: B, C, E, F, G, H, and J

- B=Reservoir Capacity (MAX)
 - C=Ordering Schedule
 - E=Allocation to each sector
 - F=Size of the Reservoirs
 - G=Generation of electricity
 - H=Hospitals and schools
 - J=Water Table
-

Performing a Resolution IV FF to the “Positive” group: B, C, E, F, G, H, J

Factors	B	C	E	F	G	H	J	Bo
TRUE	12	4	0	-8	-12	0	-4	12
EffectEstim	12.14	2.53	1.17	-7.20	-11.82	0.39	-3.49	13.59
RegCoef	6	2	0	-4	-6	0	-2	12
RegEst.	6.07	1.26	0.59	-3.60	-5.91	0.19	-1.75	6.80
Signific.	Yes	Yes	No	Yes	Yes	No	Yes	

Notice how, once all the (erroneously estimated) variables of the “same sign” were re-analyzed as a sub-group. Plackett-Burnam estimations then became closer to the True parameter values, both in sign and in magnitude.

Latin Hypercube Sampling

- Multiple regression analysis approach
 - Sampling at “best” points in sample space
 - Regression selection methods
 - To obtain most efficient Meta Model set
 - Provides a list of Alternative Meta Models
 - Some, not as efficient -but close enough
 - Their factors can be “controlled” by the user
 - Very effective modeling approach.
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Latin Hypercube Example

Assume we have a three dimensional ($p = 3$) problem in variables B, I, J (reservoir capacity; wetland size and water table use) and that these are respectively distributed Normal, Uniform and Exponential,. Assume that we want to draw a random sample of size $n = 10$. Divide each variable, according to its probability distribution, into ten equi-probable segments (Prob. = $0.1 = 1/10$), identifying each segment with integers 1 through 10.

Then, draw a random variate (r.v.) from each of the ten segments, for each of the three variables B, I, J. Finally, obtain the $10!$ permutations of integers 1 through 10. Randomly assign one of such permutations (e.g. segments 2,1,5,4,6,9,8,10,7 for B), to each of the variables, select the corresponding segment r.v., and form the vector sample, as below:

Example of Latin Hypercube Sampling Segments

Sample	1st	2nd	3rd	4th	5th	6th	7th	8th	9th	10th
B	2	3	1	5	4	6	9	8	10	7
I	4	2	7	1	5	9	10	8	6	3
J	8	6	2	7	1	5	4	3	9	10

Taguchi Methodology

- Analyzes both Location and Variation
 - Of the performance measure of interest
- Best combination of both these together
 - To obtain the most efficient Model
- Optimize Location, resilient to Variation
- Minimize Variation, resilient to Location
- Determine regions of joint optimality
- Determine Variation is NOT an issue
- Done equivalently by implementing a DOE.

Taguchi SN Ratios

The preferred parameter settings are determined through analysis of the “signal-to-noise” (SN) ratio, where factor levels that maximize appropriate SN ratio are optimal. There are three standard types of SN ratios that depend on the desired performance response:

- Smaller the better (for making system response as small as possible):

$$SN_S = -10 \cdot \text{Log}[1/n (\sum y_i^2)]$$

- Nominal the best (for reducing variability around a target):

$$SN_T = 10 \cdot \text{Log} (y^2 / s^2)$$

- Larger the better (for making system response as large as possible):

$$SN_S = -10 \cdot \text{Log}[1/n (\sum 1/y_i^2)]$$

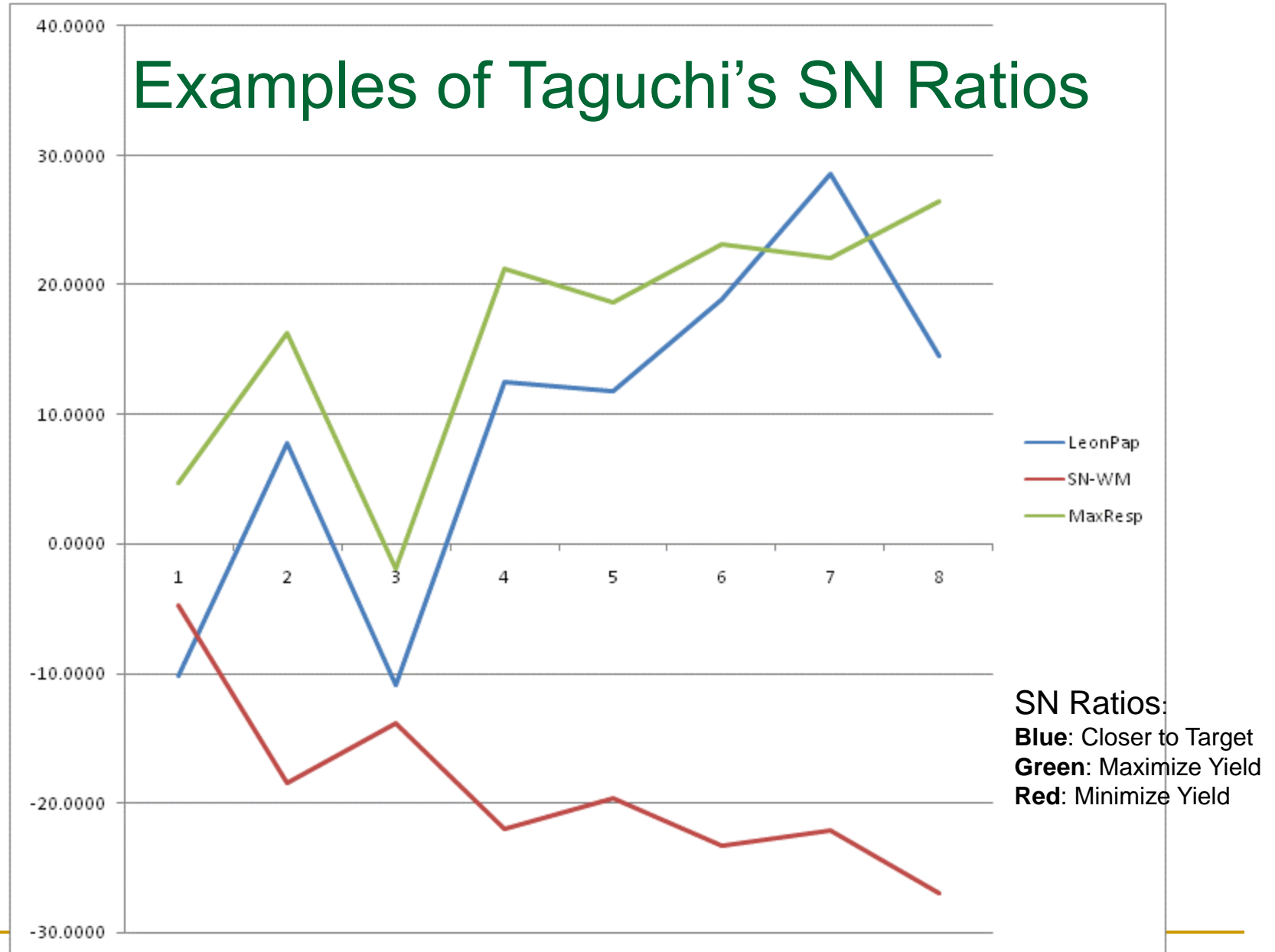
These SN ratios are derived from the quadratic loss function.

Example of Taguchi Methodology

X1	X2	X3	X4	X5	1	2	3	4	Var	LnVar	Average	TaguchiSN
1	1	1	-1	-1	194	197	193	275	1616.25	7.39	214.75	-46.75
1	1	-1	1	1	136	136	132	136	4.00	1.39	135.00	-42.61
1	-1	1	-1	1	185	261	264	264	1523.00	7.33	243.50	-47.81
1	-1	-1	1	-1	47	125	127	42	2218.92	7.70	85.25	-39.51
-1	1	1	1	-1	295	216	204	293	2376.67	7.77	252.00	-48.15
-1	1	-1	-1	1	234	159	231	157	1852.25	7.52	195.25	-45.97
-1	-1	1	1	1	328	326	247	322	1540.25	7.34	305.75	-49.76
-1	-1	-1	-1	-1	186	187	105	104	2241.67	7.71	145.50	-43.59

- **VARIABLES ANALYZED**
- Response: Wet Land Size
- X1=Reservoir Capacity (MAX)
- X2=Generation of electricity
 - X3=Hospital Capacity
 - X4=Social Services
 - X5=Fish/Foul Population
- Z1 and Z2 are two ***noise*** variables

Examples of Taguchi's SN Ratios



Analysis for Joint Location-Variance

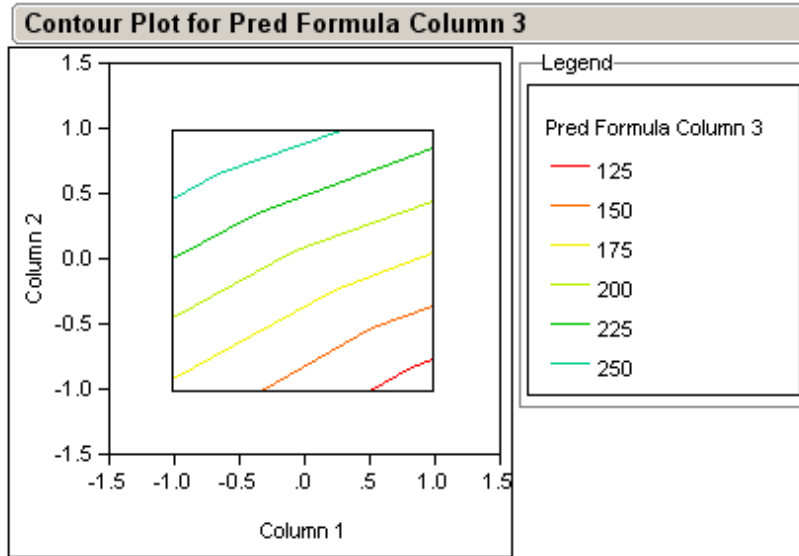
Regression Analysis for the Main Effect influence

	Coef	Std Err	t Stat	P-val	Lower 95	Upper 95
Intercept	197.13	7.88	25.01	0.00	181.00	213.25
X Var 1	-27.50	7.88	-3.49	0.00	-43.62	-11.38
X Var 2	56.88	7.88	7.21	0.00	40.75	73.00

Regression Analysis for the Variance Influence

	Coef	Std Err	t Stat	P-val	Lower 95	Upper 95
Intercept	6.77	0.78	8.70	0.00	4.77	8.77
X Var 1	-0.82	0.78	-1.05	0.34	-2.82	1.18
X Var 2	0.69	0.78	0.88	0.42	-1.31	2.69

Graphical *Combined* DOE Approach



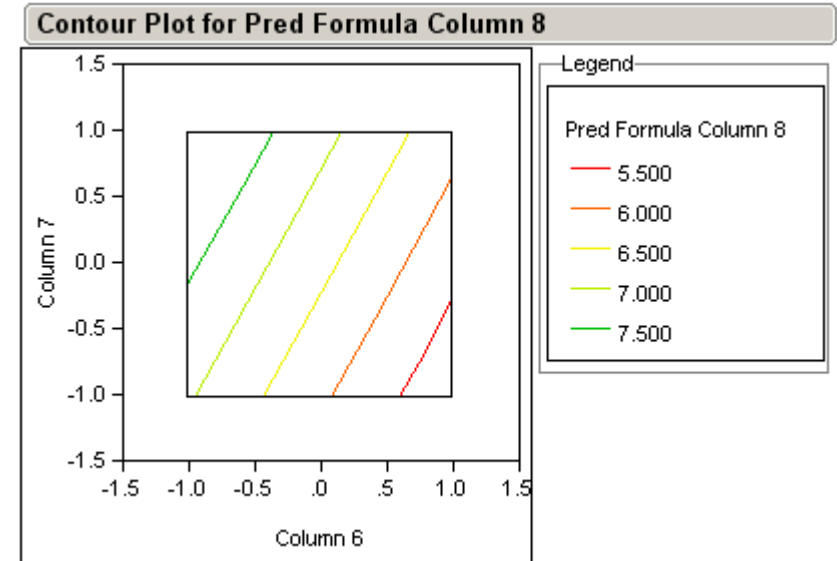
Optimal Solution:

Overlaying both plots (for location and variation) we seek to Minimize simultaneously Yield and Variation.

Jointly applying the two above (cols. 3 & 8).

The Optimum is around (1, -1), yielding

Estimated Minimum Output = 113; Min Variation = 5.3



Estimated Yield:

$$Y = 197.12 - 27.5X_1 + 56.9X_2$$

$$Y(1, -1) = 112.72$$

Estimated Variation:

$$Y = 6.77 - 0.82X_1 + 0.69X_2$$

$$Y(1, -1) = 5.26$$

Pan-American Advanced Studies Institute

Synopsis of Program:

The Pan-American Advanced Studies Institutes (PASI) Program is a jointly supported initiative between the Department of Energy (DOE) and the National Science Foundation (NSF). Pan-American Advanced Studies Institutes are short courses ranging in length from ten to twenty-one days, involving lectures, demonstrations, research seminars, and discussions at the advanced graduate, post-doctoral, and junior faculty level.

PASIs aim to disseminate advanced scientific and engineering knowledge and stimulate training and cooperation among researchers of the Americas in the mathematical, physical, and biological sciences, the geosciences, the computer and information sciences, and the engineering fields. Proposals in other areas funded by NSF may be considered on an ad hoc basis as long as they are multidisciplinary; in this case, lead investigators must consult with the PASI Program before proposal submission.

Pan-American Advanced Studies Institute

- US-Latin American Scientists/Researchers
- Modeling of Environmental Problems
- Modelers: statistics & applied math (O.R.)
- Environmental Science Specialists
- From USA: EPA, GLRC, Other Universities
- From LA: Mexico, Brazil, Argentina, Chile, Colombia, Ecuador, Puerto Rico, others
- Via the Juarez Lincoln Marti Int'l Ed. Project
 - <http://web.cortland.edu/matresearch>

Conclusions

- DOEs are complex methodologies
 - Size and interactions are serious issues
 - Existing methods, not fully compliant
 - But promise, if worked around
 - Some Models are useful
 - For strategic and tactical decisions
 - In crisis, and to assess/avoid them
 - In theoretical and applied studies
 - A PASI for Latin America in preparation
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