

MATLAB Reference Card

Operators and special characters.	
+	Plus; addition operator.
-	Minus; subtraction operator.
*	Scalar and matrix multiplication operator.
.*	Array (element-by-element) multiplication operator.
^	Scalar and matrix exponentiation operator.
.^	Array (element-by-element) exponentiation operator.
\	Left-division operator.
/	Right-division operator.
.\	Array (element-by-element) left-division operator
./	Array (element-by-element) right-division operator.
:	Colon; generates regularly spaced elements and represents an entire row or column.
()	Parentheses; encloses function arguments and array indices; overrides precedence.
[]	Brackets; encloses array elements.
{ }	Braces; encloses cell elements.
.	Decimal point.
...	Ellipsis; line-continuation operator.
,	Comma; separates statements, and elements in a row of an array.
;	Semicolon; separates columns in an array, and suppresses display.
%	Percent sign; designates a comment, and specifies formatting.
'	Quote sign and transpose operator.
.'	Non-conjugated transpose operator.
=	Assignment (replacement) operator.

Logical and relational operators.	
==	Relational operator; equal to.
~=	Relational operator, not equal to.
<	Relational operator, less than.
<=	Relational operator, less than or equal to.
>	Relational operator, greater than.
>=	Relational operator, greater than or equal to.
&	Logical operator, AND.
	Logical operator, OR.
~	Logical operator, NOT.

Order of precedence.	
Highest	Parentheses, evaluated starting with the innermost pair.
	Transpose and exponentiation, evaluated left to right.
	Unary plus or minus and logical NOT (~), evaluated left to right.
	Multiplication and division, evaluated from left to right.

	Addition and subtraction, evaluated from left to right.
	Colon operator (:).
	Relational operators, evaluated from left to right.
	Logical AND (&), evaluated left to right.
Lowest	Logical OR (), evaluated left to right.

Special variables and constants.	
ans	Most recent answer.
eps	Accuracy of floating point precision.
i, j	The imaginary unit (square root of -1).
Inf	Infinity.
NaN	Undefined numerical result (not a number).
pi	The number π .

Commands for managing a session.	
clc	Clears Command window.
clear	Removes variables from memory.
doc	Displays documentation.
exist	Checks for existence of file or variable.
global	Declares variables to be global.
help	Displays help text in the Command window.
helpwin	Displays help text in the Help Browser.
lookfor	Searches help entries for a keyword.
quit	Stops MATLAB.
who	Lists current variables.
whos	Lists current variables (long display).

System and file commands.	
cd	Changes current directory.
date	Displays current date.
delete	Deletes a file.
diary	Switches on/off diary file recording.
dir	Lists all files in current directory.
get	Returns diary status or filename.
load	Loads workspace variables from a file.
path	Displays search path.
pwd	Displays current directory.
save	Saves workspace to a file.
type	Displays contents of a file.
what	Lists all MATLAB files.
wk1read	Reads .wk1 spreadsheet file.
xlsread	Reads .xls spreadsheet file.

Input/output commands.	
disp	Displays contents of an array or string.

dlmwrite	Writes formatted data to an ASCII file.
format	Controls screen-display format.
fprintf	Performs formatted writes to screen or file.
input	Displays prompts and waits for output.
menu	Displays a menu of choices
i	Suppresses screen printing.

Numeric display formats	
format short	Four decimal digits (default)
format long	16 decimal digits.
format short e	Five digits plus exponent.
format long e	16 digits plus exponents.
format bank	Two decimal digits.
format +	Positive, negative, or zero.
format rat	Rational approximation.
format compact	Suppresses some line feeds.
format loose	Resets to less compact display mode.

Array functions	
cat	Concatenates arrays.
find	Finds indices of nonzero elements.
length	Computes number of elements.
linspace	Creates regularly spaced vector.
logspace	Creates logarithmically spaced vector.
max	Returns largest element.
min	Returns smallest element.
size	Computes array size.
sort	Sorts each column.
sum	Sums each column.

Special matrices	
eye	Creates an identity matrix.
ones	Creates an array of ones.
zeros	Creates an array of zeros.

Matrix functions for solving linear equations	
det	Computes determinant of an array.
inv	Computes inverse of a matrix.
pinv	Computes pseudo-inverse of a matrix.
rank	Computes rank of a matrix.
rref	Computes reduced row echelon form.

Exponential and logarithmic functions	
exp(x)	Exponential; e^x .
log(x)	Natural logarithm; $\ln x$.

<code>log10(x)</code>	Common (base ten) logarithm; $\log_{10}x$.
<code>sqrt(x)</code>	Square root of x .

Complex functions	
<code>abs(x)</code>	Absolute value of x .
<code>angle(x)</code>	Angle of a complex number x .
<code>conj(x)</code>	Complex conjugate of x .
<code>imag(x)</code>	Imaginary part of a complex number x .
<code>real(x)</code>	Real part of a complex number x .

Numeric functions	
<code>ceil</code>	Rounds to the nearest integer toward ∞ .
<code>fix</code>	Rounds to the nearest integer toward zero.
<code>floor</code>	Rounds to the nearest integer toward $-\infty$.
<code>round</code>	Rounds toward the nearest integer.
<code>sign(x)</code>	Returns +1, 0, or -1, depending on sign of x .

Trigonometric functions	
<code>acos(x)</code>	Inverse cosine; $\cos^{-1}x$.
<code>acot(x)</code>	Inverse cotangent; $\sec^{-1}x$.
<code>acsc(x)</code>	Inverse cosecant; $\csc^{-1}x$.
<code>asec(x)</code>	Inverse secant; $\sec^{-1}x$.
<code>asin(x)</code>	Inverse sine; $\sin^{-1}x$.
<code>atan(x)</code>	Inverse tangent; $\tan^{-1}x$.
<code>atan2(y, x)</code>	Four-quadrant inverse tangent of y/x .
<code>cos(x)</code>	Cosine; $\cos x$.
<code>cot(x)</code>	Cotangent; $\cot x$.
<code>csc(x)</code>	Cosecant; $\csc x$.
<code>sec(x)</code>	Secant; $\sec x$.
<code>sin(x)</code>	Sine; $\sin x$.
<code>tan(x)</code>	Tangent; $\tan x$.

Hyperbolic functions	
<code>acosh(x)</code>	Inverse hyperbolic cosine; $\cosh^{-1}x$.
<code>acoth(x)</code>	Inverse hyperbolic cotangent; $\coth^{-1}x$.
<code>acsch(x)</code>	Inverse hyperbolic cosecant; $\operatorname{csch}^{-1}x$.
<code>asech(x)</code>	Inverse hyperbolic secant; $\operatorname{sech}^{-1}x$.
<code>asinh(x)</code>	Inverse hyperbolic sine; $\sinh^{-1}x$.
<code>atanh(x)</code>	Inverse hyperbolic tangent; $\tanh^{-1}x$.
<code>cosh(x)</code>	Hyperbolic cosine; $\cosh x$.
<code>coth(x)</code>	Hyperbolic cotangent; $\cosh x / \sinh x$.
<code>csch(x)</code>	Hyperbolic cosecant; $1 / \sinh x$.
<code>sech(x)</code>	Hyperbolic secant; $1 / \cosh x$.
<code>sinh(x)</code>	Hyperbolic sine; $\sinh x$.
<code>tanh(x)</code>	Hyperbolic tangent; $\sinh x / \cosh x$.

Polynomial functions	
conv	Computes product (convolution) of two polynomials.
deconv	Computes ratio (deconvolution) of polynomials.
eig	Computes the eigenvalues of a matrix.
poly	Computes polynomial from roots.
polyfit	Fits a polynomial to data.
polyval	Evaluates polynomial.
roots	Computes polynomial roots.

String functions	
findstr	Finds occurrences of a string.
strcmp	Compares strings.

Logical Functions	
any	True if any elements are nonzero.
all	True if all elements are nonzero.
find	Finds indices of nonzero elements.
finite	True if elements are finite.
isnan	True if elements are undefined.
isempty	True if elements are infinite.
isreal	True if elements are real.
xor	Exclusive OR.

Miscellaneous mathematical functions	
cross	Computes cross products.
dot	Computes dot products.
function	Creates a user-defined function.

Cell array functions	
cell	Creates cell array.
celldisp	Displays cell array.
cellplot	Displays graphical representation of cell array.
num2cell	Converts numeric array to cell array.
deal	Matches input and output lists.
iscell	Identifies cell array.

Structure functions	
fieldnames	Returns field names in a structured array.
getfield	Returns field contents of a structure array.
isfield	Identifies a structure field array.
isstruct	Identifies a structure array.
rmfield	Removes a field from a structure array.
setfield	Sets contents of a field.
struct	Creates structure array.

Basic xy plotting commands	
axis	Sets axis limits.
fplot	Intelligent plotting of functions.
ginput	Reads coordinates of the cursor position.
grid	Displays gridlines.
plot	Generates x-y plot.
print	Prints plot or saves to a file.
title	Puts text at top of plot.
xlabel	Adds text label to x-axis.
ylabel	Adds text label to y-axis.

Plot-enhancement commands	
axes	Creates axes objects.
gtext	Enables label placement by mouse.
hold	Freezes current plot.
legend	Legend placement by mouse.
refresh	Redraws current figure window.
set	Specifies properties of objects such as axes.
subplot	Creates plots in sub-windows.
text	Places string in figure.

Specialized plot functions	
bar	Creates bar chart.
loglog	Creates log-log plot.
plotyy	Enables plotting on left and right axes.
polar	Creates polar plot.
quiver	Plot velocity vectors as arrows.
semilogx	Creates semilog plot (logarithmic abscissa).
semilogy	Creates semilog plot (logarithmic ordinate).
stairs	Creates stair plot.
stem	Creates stem plot.

Three-dimensional plotting functions	
contour	Creates contour plot.
mesh	Creates 3D mesh surface plot.
meshc	Same as mesh with contour plot underneath.
meshz	Same as mesh with vertical lines underneath.
plot3	Creates 3D plots from lines and points.
surf	Creates shaded 3D mesh surface plot.
surfc	Same as surf with contour plot underneath.
meshgrid	Creates rectangular grid.
waterfall	Same as mesh with mesh lines in one direction.
zlabel	Adds text label to z-axis.

Program flow control	
break	Terminates execution of a loop.
case	Provides alternate execution path within switch structure.
continue	Passes control to the next iteration of a for or while loop.
else	Delineates alternate block of statements.
elseif	Conditionally executes statements.
end	Terminates for, while, and if statements.
for	Repeats statements a specific number of times.
if	Executes statements conditionally.
otherwise	Provides optional control within a switch structure.
switch	Directs program execution by comparing input with case expressions.
while	Repeats statements an indefinite number of times.

Optimization and root-finding functions	
fminbnd	Finds the minimum of a function of one variable.
fminsearch	Finds the minimum of a multivariable function.
fminunc	Finds the unconstrained minimum of a multivariable function
fmincon	Finds the minimum of a multivariable function with constraints.
fzero	Finds the zero of a function.
optimset	Creates optimization options structure.

Histogram functions	
bar	Creates a bar chart.
hist	Aggregates the data into bins.

Statistical functions	
cumsum	Computes the cumulative sum across a row.
erf(x)	Computes the error function, erf(x).
mean	Computes the mean.
median	Computes the median.
std	Computes the standard deviation.

Random number functions	
rand	Generates uniformly distributed random numbers between 0 and 1; sets and retrieves the state.
randn	Generates normally distributed random numbers; sets and retrieves the state.
randperm	Generates random permutations of integers.

Polynomial functions	
poly	Computes the coefficients of a polynomial and its roots.
polyfit	Fits a polynomial to data.
polyval	Evaluates a polynomial and generates error estimates.

roots	Computes the roots of a polynomial from its coefficients.
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Interpolation functions	
interp1	Linear and cubic-spline interpolation of a uni-variable function.
interp2	Linear interpolation of a function of two variables.
spline	Cubic-spline interpolation.
unmkpp	Computes the coefficients of cubic-spline polynomials.

Numerical differentiation and integration functions	
diff(x)	Computes the differences between adjacent elements in a vector x
polyder	Differentiates a polynomial, a polynomial product, or a polynomial quotient.
quad	Numerical integration with adaptive Simpson's rule.
quadl	Numerical integration with Lobatto quadrature.
trapz	Numerical integration with the trapezoidal rule.

ODE solvers	
ode23	Nonstiff, low-order solver.
ode45	Nonstiff, medium-order solver.
ode113	Nonstiff, variable-order solver.
ode23s	Stiff, low-order solver.
ode23t	Moderately-stiff, trapezoidal rule solver.
ode23tb	Stiff, low-order solver.
ode15s	Stiff, variable-order solver.
odeset	Creates integrator options structure for ODE solvers.

Predefined input functions	
gensig	Generates a periodic sine, square, or pulse input.
sawtooth	Generates a periodic sawtooth input.
square	Generates a square wave input.
stepfun	Generates a step function input.

Functions for creating and evaluating symbolic expressions	
class	Returns the class of an expression.
digits	Sets the number of decimal digits used to do variable precision arithmetic.
double	Converts an expression to numeric form.
ezplot	Generates a plot of a symbolic expression.
findsym	Finds the symbolic variables in a symbolic expression.
numden	Returns the numerator and denominator of an expression.
sym	Creates a symbolic variable.
syms	Creates one or more symbolic variables.
vpa	Sets the number of digits used to evaluate expressions.

Functions for manipulating symbolic expressions	
collect	Collects coefficients of like powers in an expression
expand	Expands an expression by carrying out powers.
factor	Factors an expression.
poly2sym	Converts a polynomial coefficient vector to a symbolic polynomial.
pretty	Displays an expression in a form that resembles typeset mathematics.
simple	Searches for the shortest form of an expression.
simplify	Simplifies an expression using Maple's simplification rules.
subs	Substitutes variables or expressions.
sym2poly	Converts an expression to a polynomial coefficient vector.

Symbolic solution of equations	
solve	Solves symbolic equations.
dsolve	Returns the symbolic solution of a differential equation or set of equations.

Symbolic calculus functions	
diff	Returns the derivative of an expression.
dirac	Dirac delta function (unit impulse).
heaviside	Heaviside function (unit step).
int	Returns the integral of an expression.
limit	Returns the limit of an expression.
symsum	Returns the symbolic summation of an expression.
taylor	Returns the Taylor series of a function.

Symbolic linear algebra functions	
det	Returns the determinant of a matrix.
eig	Returns the eigenvalues (characteristic values) of a matrix.
inv	Returns the inverse of a matrix.
poly	Returns the characteristic polynomial of a matrix.

Laplace transform functions	
ilaplace	Returns the inverse Laplace transform.
laplace	Returns the Laplace transform.

Sample Program (Lecture02a.m)

```
function Lecture02a()
% Lecture02a - this program simulates UNSsteady 1d heat
% CONDDuction with (unsteady) temperatures prescribed at the boundaries
%
% written by John Dannenhoffer

clear

% get all inputs
xmax = input('Enter xmax: ');           % maximum depth (m)
I = input('Enter I: ');                 % number of points in i direction (-)
tmax = input('Enter tmax: ');           % maximum time (d)
N = input('Enter N: ');                 % maximum number of time steps (-)

alfa = 0.52 * 3600 * 24 / 2050 / 1840; % diffusivity (m2/d)
fprintf(1, 'Enter alfa: %f\n', alfa);

dx = xmax / I;                          % distance between nodes (m)
dt = tmax / N;                            % time step (d)

II = I + 1;
NN = N + 1;

Fo = alfa * dt / (dx^2);                  % Fourier number

% set up space array and initial temperatures
for ii = 1 : II
    nn = 1;
    x(ii) = (ii-1) * dx;                  % spatial position (m)
    t(ii, nn) = 0;                        % initial time (d)
    T(ii, nn) = 20;                       % initial temperature (C)
end % for ii

% step through remaining times
for nn = 2 : NN
    t(nn) = (nn-1) * dt;

    % set up the coefficients...

    % ...left boundary condition
    atri(1) = 1;
    btri(1) = 0;
    ctri(1) = 0;
    if (t(nn) < 60)                       % left boundary temperature (C)
        dtri(1) = -15;
    else
        dtri(1) = +20;
    end % if

    % ...interior (governing equation)
    for ii = 2 : II-1
        atri(ii) = 1 + 2 * Fo;
        btri(ii) = - Fo;
        ctri(ii) = - Fo;
        dtri(ii) = T(ii, nn-1);
    end % for ii

    % ...right boundary condition
    atri(II) = 1;
    btri(II) = 0;
    ctri(II) = 0;
    dtri(II) = 20;                         % right boundary temperature (C)

    % use the Thomas algorithm to solve the tridiagonal system
    Tnew = thomas(II, atri, btri, ctri, dtri);

    % put the "results" into the temperature array
    for ii = 1 : II
```

```

        T(ii,nn) = Tnew(ii);
    end % for ii
end % for nn

% find the minimum depth for which T > 0
mindepth = x(II);

for ii = II-1 : -1 : 1
    okay = 1;

    for nn = 1 : NN
        if (T(ii,nn) < 0)
            okay = 0;
        end % if
    end % for nn

    if (okay == 1)
        mindepth = x(ii);
    end % if
end % for ii

fprintf(1, '\nMinimum depth that pipe can be buried is approximately %f(m)\n', mindepth);

% plot a contour of the results
for nn = 1 : NN
    for ii = 1 : II
        tt(ii,nn) = t(nn);
        xx(ii,nn) = x(ii);
    end % for ii
end % for nn

[cs,h] = contourf(xx, tt, T); ...
    colorbar
    title('Contours of temperature (C)')
    xlabel('x (m)')
    ylabel('t (d)')

%-----

function x = thomas(n, a, b, c, d);
% THOMAS Solve a tridiagonal matrix using the Thomas algorithm
%
% [a1  c1           ] [x1]  [d1]
% [b2  a2  c2       ] [x2]  [d2]
% [   b3  a3  c3    ] [x3]  [d3]
% [           ...   ] [. ]  [. ]
% [           bn  an ] [xn]  [dn]
%
% inputs:
%   n           size of matrix
%   a           array of diagonal elements
%   b           array of subdiagonal elements
%   c           array of superdiagonal elements
%   d           array of right-hand sides
% output:
%   x           array of solutions

% Forward elimination

p(1) = - c(1) / a(1);
q(1) =  d(1) / a(1);

for i = 2 : n
    p(i) = - b(i) / (a(i) + c(i) * p(i-1));
    q(i) = ( d(i) - c(i) * q(i-1)) / (a(i) + c(i) * p(i-1));
end % for i

% Back substitution

```

```
x(n) = q(n);  
for i = n-1 : -1 : 1  
    x(i) = p(i) * x(i+1) + q(i);  
end % for i%
```